

**Technische Universität Graz**



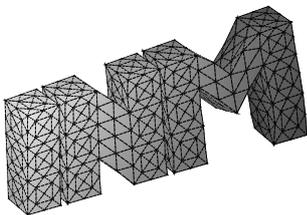
---

12. Workshop on  
**Fast Boundary Element Methods in  
Industrial Applications**

Söllnerhaus, 25.–28.9.2014

U. Langer, M. Schanz, O. Steinbach, W. L. Wendland (eds.)

---



**Berichte aus dem  
Institut für Numerische Mathematik**



# Technische Universität Graz

---

12. Workshop on  
Fast Boundary Element Methods in  
Industrial Applications

Söllerauhaus, 25.–28.9.2014

U. Langer, M. Schanz, O. Steinbach, W. L. Wendland (eds.)

---

## Berichte aus dem Institut für Numerische Mathematik

Book of Abstracts 2014/8

Technische Universität Graz  
Institut für Numerische Mathematik  
Steyrergasse 30  
A 8010 Graz

**WWW:** <http://www.numerik.math.tu-graz.ac.at>

© Alle Rechte vorbehalten. Nachdruck nur mit Genehmigung des Autors.

## Program

Thursday, September 25, 2014	
15.30	Coffee
18.30	Dinner
Friday, September 26, 2014	
9.00–9.30	J. Dölz (Basel, Switzerland) $\mathcal{H}$ -matrix accelerated second moment analysis for potentials with rough correlation
9.30–10.00	D. Lukas (Ostrava, Czech Republic) A boundary element method for homogenization
10.00–10.30	N. Salles (London, UK) New analytical results on the convergence of a convolution quadrature method
10.30–11.00	Coffee
11.00–11.30	E. van't Wout (London, UK) Simulation of high intensity focused ultrasound with BEM++ and the Laplace–Beltrami preconditioner
11.30–12.00	C. Urzua–Torres (Zürich, Switzerland) Dual–preconditioning for boundary integral equations on screens
12.00–12.30	T. Führer (Vienna, Austria) Optimal preconditioning for the coupling of adaptive finite and boundary elements
12.30	Lunch
15.00–15.30	Coffee
17.00–17.30	M. Aussal (Palaiseau, France) The sparse cardinal sine decomposition and its application to fast boundary element method
17.30–18.00	G. Gantner (Vienna, Austria) Reliable and efficient a posteriori error estimation for adaptive IGA boundary element methods for weakly singular integral equations
18.30	Dinner

Saturday, September 27, 2014	
9.00–9.30	S. Kurz (Tampere, Finland) Structure preserving mesh coupling for Maxwell's equations
9.30–10.00	D. Amann (Graz, Austria) Helmholtz transmission problem for composite structures
10.00–10.30	G. Unger (Graz, Austria) Boundary element methods for Maxwell's eigenvalue problem
10.30–11.00	Coffee
11.00–11.30	W. L. Wendland (Stuttgart, Germany) tba
11.30–12.00	Jan Zapletal (Ostrava, Czech Republic) Shape optimization based on BEM and subdivision surfaces
12.00–12.30	M. Bugeanu (Basel, Switzerland) A second order convergent trial method for free boundary problems
12.30	Lunch
13.30–18.00	Hiking Tour
18.30	Dinner
Sunday, September 28, 2014	
9.00–9.30	H. Harbrecht (Basel, Switzerland) The $\mathcal{H}^2$ wavelet method
9.30–10.00	O. Steinbach (Graz, Austria) Space-time finite and boundary element methods for parabolic initial boundary value problems
10.00–10.30	Closing and Coffee

13. Söllerhaus Workshop on  
**Fast Boundary Element Methods in Industrial Applications**  
September 27–30, 2015

## **Helmholtz transmission problem for composite structures**

D. Amann, O. Steinbach

TU Graz, Austria

When solving transmission problems for the Helmholtz equation using boundary integral equations, eigenvalues of the interior Laplace operator, so called spurious modes, may cause difficulties. If they appear, certain boundary integral operators lose their injectivity. The existence of spurious modes depends on the wave numbers as well as on the domains.

In this work we consider the case of a Lipschitz domain with a piecewise constant wave number. For this model problem we review and discuss three formulations that overcome the problem mentioned above, which means we can establish unique solvability for all wave numbers. The presented formulations are the classic combined boundary integral formulation, the Steklov–Poincaré operator formulation and the local multitrace formulation. Since we want to efficiently apply iterative solvers, we examine if these approaches are compatible to preconditioning strategies and how preconditioners can be constructed. Finally numerical examples are presented to support our findings and compare the three formulations.

# The sparse cardinal sine decomposition and its application to fast boundary element method

F. Alouges and M. Aüssal  
École Polytechnique, Palaiseau, France

Fast convolution algorithms on unstructured grids have become a well established subject. Algorithms such as Fast Multipole Method (FMM), adaptive cross approximation (ACA) or H-matrices for instance are, by now, classical and reduce the complexity of the matrix-vector product from  $O(N^2)$  to  $O(N \log N)$  with a broad range of applications in e.g. electrostatics, magnetostatics, acoustics or electromagnetics.

In this talk we describe a new numerical method [1] which is based on a suitable Fourier decomposition of the Green kernel, associated to sparse quadrature formulae. We show how the approach uses the so-called Type-III Non Uniform Fast Fourier Transform (NUFFT) [4,5], to perform efficiently the convolution. Applications for tri-dimensional Laplace and Helmholtz kernel are provided, both in collocation and Finite Element approximations. A comparison with the FMM [2,3] shows a similar complexity scaling. Eventually, we present the acoustics scattering by a human head, which is of particular importance for 3D- Audio solutions.

## References

- [1] Alouges, F., Aüssal, M. (2014) *The Sparse Cardinal Sine Decomposition and its application for fast numerical convolution*. Submitted.
- [2] Greengard, L., & Rokhlin, V. (1987). *A fast algorithm for particle simulations*. Journal of computational physics, 73(2), 325-348.
- [3] Greengard, L. (1988). *The rapid evaluation of potential fields in particle systems*. MIT press.
- [4] Greengard, L., & Lee, J. Y. (2004). *Accelerating the nonuniform fast Fourier transform*. SIAM review, 46(3), 443-454.
- [5] Lee, J. Y., & Greengard, L. (2005). *The type 3 nonuniform FFT and its applications*. Journal of Computational Physics, 206(1), 1-5.

## **A second order convergent trial method for free boundary problems**

Mihaela Monica Bugeanu and Helmut Harbrecht

Universität Basel, Switzerland

In this talk, we will present a method for solving the Bernoulli free boundary problem using a trial method of second order convergence. For the free boundary, we impose the Neumann boundary condition and use the Dirichlet boundary data for the update. We will first present the method in question and then show numerical results that support the claim of a second order convergent method.

## **$\mathcal{H}$ -matrix accelerated second moment analysis for potentials with rough correlation**

Jürgen Dölz<sup>1</sup>, Helmut Harbrecht<sup>1</sup>, Michael Peters<sup>1</sup>, Christoph Schwab<sup>2</sup>

<sup>1</sup>Universität Basel, Switzerland,   <sup>2</sup>ETH Zürich, Switzerland

We consider the efficient solution of strongly elliptic potential problems with stochastic Dirichlet data by the boundary integral equation method. The computation of the solution's two-point correlation is well understood if the two-point correlation of the Dirichlet data is known and sufficiently smooth. Unfortunately, the problem becomes much more involved in case of rough data. We will show that the concept of the H-matrix arithmetic provides a powerful tool to cope with this problem. By employing a parametric surface representation, we end up with an H-matrix arithmetic based on balanced cluster trees. This considerably simplifies the implementation and improves the performance of the H-matrix arithmetic. Numerical experiments are provided to validate and quantify the presented methods and algorithms.

# Optimal preconditioning for the coupling of adaptive finite and boundary elements

M. Feischl<sup>1</sup>, T. Führer<sup>1</sup>, D. Praetorius<sup>1</sup>, E. P. Stephan<sup>2</sup>

<sup>1</sup>TU Vienna, Austria, <sup>2</sup>Leibniz University, Hannover, Germany

For many relevant applications, the coupling of the finite element method (FEM) and boundary element method (BEM) appears to be the appropriate numerical method to cope with unbounded domains. As the problem size increases, so does the strong need for effective preconditioners for iterative solvers. Most of the available literature on preconditioning of FEM-BEM coupling techniques deals with the symmetric coupling on quasi-uniform meshes. Often, however, non-symmetric coupling formulations are preferred, since they avoid the computation and evaluation of the hypersingular integral operator.

We present results [1] on block-diagonal preconditioning for the Johnson-Nédélec coupling on adaptively generated meshes. With an appropriate stabilization vector  $\mathbf{S}$ , which ensures positive definiteness of the coupling formulation, the Galerkin matrix of the Johnson-Nédélec coupling reads in block form

$$\begin{pmatrix} \mathbf{A} & -\mathbf{M}^T \\ \frac{1}{2}\mathbf{M} - \mathbf{K} & \mathbf{V} \end{pmatrix} + \mathbf{S}\mathbf{S}^T,$$

where  $\mathbf{A}$  corresponds to the FEM part,  $\mathbf{V}$  resp.  $\mathbf{K}$  to the discrete simple-layer resp. double-layer integral operator and  $\mathbf{M}$  is the mass matrix. We consider block-diagonal preconditioners

$$\begin{pmatrix} \mathbf{P}_{\text{FEM}} & \mathbf{0} \\ \mathbf{0} & \mathbf{P}_{\text{BEM}} \end{pmatrix},$$

where the diagonal blocks  $\mathbf{P}_{\text{FEM}}$  and  $\mathbf{P}_{\text{BEM}}$  are symmetric and positive definite. These are obtained from a local multilevel additive Schwarz decomposition of the energy space. While the analysis relies on this abstract frame, the resulting preconditioners are obtained from simple algebraic postprocessing of the (history of the) Galerkin matrix.

Starting from an initial mesh which is adaptively refined by bisection, we prove that the condition number of the preconditioned system remains bounded, where the bound depends only on the initial mesh.

Although we shall mainly discuss the 2D Laplace transmission problem, the principal ideas also apply to the 3D case and Lamé-type transmission problems. Moreover, the analysis transfers to other coupling methods, such as the symmetric coupling or the symmetric and non-symmetric Bielak-MacCamy coupling.

## References

- [1] M. Feischl, T. Führer, D. Praetorius, E. P. Stephan. Optimal preconditioning for the symmetric and non-symmetric coupling of adaptive finite elements and boundary elements. *ASC Report 36/2013, Vienna University of Technology*, 2013.

# Reliable and efficient a posteriori error estimation for adaptive IGA boundary element methods for weakly-singular integral equations

M. Feischl, G. Gantner, D. Praetorius

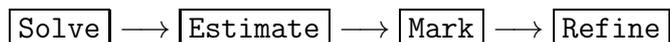
TU Vienna, Austria

A posteriori error estimation and adaptive mesh-refinement are well-established and important tools for standard boundary element methods (BEM) for polygonal boundaries and piecewise polynomial ansatz functions. In contrast, the mathematically reliable a posteriori error analysis for isogeometric BEM (IGABEM) has not been considered, yet. In our talk, we aim to shed some light on this gap and to transfer some known results on reliable a posteriori error estimators from standard BEM to IGABEM.

As model example serves the weakly-singular integral equation for the 2D Laplacian. For our IGABEM, we employ non-uniform rational B-splines (NURBS). With  $\phi$  denoting the exact solution and  $\Phi_\ell$  being the discrete IGABEM solution, we prove in [2] that the (numerically computable) Faermann error estimator  $\eta_\ell$ , proposed and analyzed in [1] for standard BEM, provides lower and upper bounds for the (in general, non-computable and unknown) error in the  $H^{-1/2}$ -energy norm, i.e.,

$$C_{\text{eff}}^{-1} \eta_\ell \leq \|\phi - \Phi_\ell\| \leq C_{\text{rel}} \eta_\ell.$$

We prove that the constants  $C_{\text{eff}}, C_{\text{rel}} > 0$  remain bounded even if new knots are inserted resp. the multiplicity of knots is increased. In particular,  $\eta_\ell$  can thus be used to monitor the error decay if the mesh is refined. Moreover, the local contributions of  $\eta_\ell$  can be used for adaptive IGABEM computations to steer an adaptive algorithm of the form



which automatically detects singularities of the solution and adapts the mesh accordingly. If compared to uniform mesh refinement, this dramatically reduces the storage requirements as well as the computing time needed to achieve a certain prescribed accuracy.

## References

- [1] Birgit Faermann. Localization of the Aronszajn-Slobodeckij norm and application to adaptive boundary element methods, part I. The two-dimensional case. *IMA J. Numer. Anal.*, 20(2):203–234, 2000.
- [2] M. Feischl, G. Gantner, D. Praetorius. Reliable and efficient a posteriori error estimation for adaptive IGA boundary element methods for weakly-singular integral equations, *ASC Report 23/2014, Vienna University of Technology*, 2014.

## The $\mathcal{H}^2$ -wavelet method

Daniel Alm, Helmut Harbrecht, Ulf Krämer  
Universität Basel, Switzerland

Abstract: We introduce the  $\mathcal{H}^2$ -wavelet method for the fast solution of nonlocal operator equations on unstructured meshes. On the given mesh, we construct a wavelet basis which provides vanishing moments with respect to the traces of polynomials in the space. With this basis at hand, the system matrix in wavelet coordinates is compressed to  $(N \log N)$  relevant matrix coefficients, where  $N$  denotes the number of boundary elements. The compressed system matrix is computed with nearly linear complexity by using the  $\mathcal{H}^2$ -matrix approach. Numerical results in three spatial dimensions validate that we succeeded in developing a fast wavelet Galerkin scheme on unstructured triangular or quadrangular meshes.

## Structure Preserving Mesh Coupling for Maxwell's Equations

Ossi Niemimäki, Stefan Kurz, Lauri Kettunen  
Tampere University of Technology, Finland

The state of the art for mesh coupling at nonconforming interfaces is presented and reviewed. Mesh coupling is frequently applied to the modeling and simulation of motion in electromagnetic actuators. The focus of the contribution is on lowest order Whitney elements. Both interpolation- and projection-based methods are considered. In addition to accuracy and efficiency, we emphasize the question whether the schemes preserve the structure of de Rham complex, which underlies Maxwell's equations. As a new contribution, a structure preserving projection method is presented, in which mortar spaces are chosen from the Buffa-Christiansen complex. This approach is structure preserving. Its performance is compared with a straightforward interpolation based on Whitney and de Rham maps.

### References

- [1] Lange E, Henrotte F, Hameyer K. Biorthogonal shape functions for nonconforming sliding interfaces in 3-D electrical machine FE models with motion. *IEEE Transactions on Magnetics* Feb 2012; 48(2):855–858.
- [2] Rapetti F, Buffa A, Bouillault F, Maday Y. Simulation of a coupled magneto-mechanical system through the sliding-mesh mortar element method. *COMPEL – The International Journal for Computation and Mathematics in Electrical and Electronic Engineering* 2000; 19(2):332–340.
- [3] Journeaux A, Bouillault F, Roger J. Reducing the cost of mesh-to-mesh data transfer. *IEEE Transactions on Magnetics* Feb 2014; 50(2):437–440.
- [4] Wohlmuth B. A comparison of dual Lagrange multiplier spaces for mortar Finite Element discretizations. *ESAIM: Mathematical Modelling and Numerical Analysis* Nov 2002; 36(6):995–1012.
- [5] Bouillault F, Buffa A, Maday Y, Rapetti F. The mortar edge element method in three dimensions: application to magnetostatics. *SIAM J. Sci. Comput.* 2003; 24(4):1303–1327.
- [6] Gander MJ, Japhet C. Algorithm 932 PANG: Software for Non-Matching Grid Projections in 2d and 3d with Linear Complexity. *ACM Transactions on Mathematical Software* Mar 2013; 9(4):39:1–39:25.
- [7] Journeaux A, Nemitz N, Moreau O. Locally conservative projection methods: benchmarking and practical implementation. *COMPEL – The International Journal for Computation and Mathematics in Electrical and Electronic Engineering* Jan 2014; 33(1/2).
- [8] Hu Q, Shu S, Zou J. A mortar edge element method with nearly optimal convergence for three-dimensional Maxwell's equations. *Mathematics of Computation* Jul 2008; 77(263):1333–1353.

- [9] Ben Belgacem F, Buffa A, Maday Y. The mortar finite element method for 3D Maxwell equations: first re-sults. *SIAM J. Numer. Anal.* 2001; 39(3):880–901.
- [10] Hoppe R. Mortar edge element methods in R3. *East-West J. Numer. Math.* 1999; 7(3):159–173.
- [11] Buffa A, Maday Y, Rapetti F. Applications of the mortar element method to 3D electromagnetic moving structures. *Computational Electromagnetics, Lecture Notes in Computational Science and Engineering*, vol. 28. Springer-Verlag, 2003; 35–50.
- [12] Buffa A, Christiansen S. A dual finite element complex on the barycentric refinement. *Mathematics of Computation* Oct 2007; 76(260):1743–1769.

## A Boundary Element Method for Homogenization

D. Lukáš, J. Bouchala, and M. Theuer  
TU VSB Ostrava, Czech Republic

Homogenized coefficients of periodic structures are calculated via an auxiliary partial differential equation in the periodic cell. Typically a volume finite element discretization is employed for the numerical solution. In this talk we reformulate the problem as a boundary integral equation using Steklov-Poincaré operators. The resulting boundary element method discretizes boundary of the periodic cell and the interface between materials within the cell. Under smoothness assumptions we prove that the homogenized coefficients converge quadratically with the mesh size. We support the theory with examples.

### References

- [1] Lukáš, D., Bouchala, J., and Theuer, M.: A boundary element method for homogenization. *Mathematics and Computers in Simulation*. To be submitted.

## **New analytical results on the convergence of a Convolution Quadrature method**

Timo Betcke, Nicolas Salles

University College, London, UK

We present new analytical results on the convergence of the numerical solution of wave problems computed using a Convolution Quadrature method with a multistep scheme. Instead of applying the Laplace transform at the beginning, we discretize using a multistep scheme, and then we perform a Z-Transform of the discrete time-steps. It results a range of modified Helmholtz problems in the Laplace domain. We prove that the numerical solution obtained with this method can converge exponentially to the exact solution of the underlying time-stepping solution.

The rate of convergence relies upon the analyticity of the frequency solutions which depends on the location of the scattering poles of the related modified Helmholtz problem, so on the integral formulation involved, and on the contour used to apply the inverse Z-Transform. Numerical results obtained using BEM++ and a time-domain toolbox are presented.

## **Space–time finite and boundary element methods for parabolic initial boundary value problems**

O. Steinbach

TU Graz, Austria

In most cases, finite and boundary element methods for time–dependent partial differential equations rely on time–stepping schemes. Although such an approach allows for a subsequent solution of the discrete system, it may not reflect the behavior of the solution properly, at least from an approximation point of view. For the model problem of the heat equation we will consider finite and boundary element methods with respect to general decompositions of the space–time domain and its boundary into finite and boundary elements, respectively. In particular, such an approach allows for an adaptive refinement simultaneously in space and time. Moreover, the global solution of the overall space–time system can be done in parallel, in contrast to more standard time discretization schemes. Here we will present a stability and error analysis of space–time finite and boundary element methods, and we present some numerical results which indicate the potential of the proposed approach.

## Boundary element methods for Maxwell's eigenvalue problem

Gerhard Unger  
TU Graz, Austria

In [1,2] boundary element approaches for Maxwell's eigenvalue problem for bounded domains were suggested. Numerical examples in these papers indicate a spectrally correct approximation of Maxwell's eigenvalue problem by the boundary element method when Raviart-Thomas elements are used. An analysis of the boundary integral formulations and their numerical approximations was not given there. In this talk we address these issues and consider Maxwell's eigenvalue problem also in unbounded domains. We analyze boundary integral formulations of Maxwell's eigenvalue problem in the framework of eigenvalue problems for holomorphic Fredholm operator-valued functions. General numerical results of this theory are applied to the Galerkin discretization of boundary integral formulations of Maxwell's eigenvalue problem.

### References

- [1] M. Durán, J.-C. Nédélec, and S. Ossandón. An efficient Galerkin BEM to compute high acoustic eigenfrequencies. *J. Vib. Acoust.*, 131(3):(31001)1–9, 2009.
- [2] Ch. Winers, J. Xin. Boundary element approximation for Maxwell's eigenvalue problem. *Math. Methods Appl. Sci.*, 36(18):2524–2539, 2013.

## Dual-preconditioning for boundary integral equations on screens

Ralf Hiptmair, Carlos Jerez-Hanckes, Carolina Urzúa-Torres  
Seminar for Applied Mathematics, ETH Zurich, Switzerland

Operator preconditioning [2,3] based on Calderón identities breaks down when considering open boundaries as when modeling screens. On the one hand, the double layer operator and its adjoint disappear. On the other hand, the associated weakly singular and hypersingular operators no longer map fractional Sobolev spaces in a dual fashion but degenerate into different subspaces depending on their extensibility by zero.

In this presentation, we review our dual-preconditioning technique for the Laplacian in 2D [4] and its extensions. Moreover, we discuss some first results for dual-preconditioning over three-dimensional screens using Buffa and Christiansen's approach [1].

### References

- [1] Buffa, A., and Christiansen, S. A dual finite element complex on the barycentric refinement. *Mathematics of Computation*. (76), pp. 1743–1769, 2007
- [2] Hiptmair, R. Operator Preconditioning. *Computers and Mathematics with Applications*. (52), pp. 699-706, 2006.
- [3] McLean, W., and Steinbach, O. Boundary element preconditioners for a hypersingular integral equation on an interval. *Advances in Computational Mathematics*. (11), pp. 271-286, 1999.
- [4] Hiptmair, R., Jerez-Hanckes, C. and Urzúa-Torres C. Mesh-independent operator preconditioning for boundary elements on open curves. (To appear in: *SIAM J. on Numerical Analysis*).

## On the coupled Darcy-Stokes flow

W. L. Wendland

Universität Stuttgart, Germany

In this lecture we consider existence, uniqueness and the construction of the viscous flow in  $\mathbb{R}^3$  around and through a bounded region consisting of different porous materials. The flow is modeled by Darcy flow in a given bounded domain and Stokes flow in the exterior  $c$  coupled on the boundary surface by continuous transmission of normal velocities whereas the pressure and the tangential velocities of the exterior Stokes flow satisfy the Beavers–Joseph conditions. The problem can be formulated in terms of potential theory based on surface potentials with charges on the boundary surface and a corresponding system of boundary potential operators of various types which defines a system of singular Fredholm integral equations for the charges?. This system of equations can be solved in appropriate Sobolev spaces which provides the construction of the solution to the flow problem.

This is joint work with Mirela Kohr (Babeş–Bolyai Univ., Cluj–Napoca, Romania) and Raja Sekhar (IIT Kharagpur, India).

## Simulation of high intensity focused ultrasound with BEM++ and the Laplace-Beltrami preconditioner

E. van 't Wout, S. Arridge, T. Betcke, P. Gelat

University College London, UK

The use of High-Intensity Focused Ultrasound (HIFU) is an important medical procedure to treat diseased tissue. An array of ultrasound beams can be designed such that it focuses on a small region. The high intensity concentrated in this area heats the tissue until a level is reached in which the disease will be destroyed. The accurate focusing becomes complicated when the diseased tissue is located near a rib cage due to reflections of the ultrasound beams. In this paper we will simulate the scattering of ultrasound on a rib cage with the open-source boundary element method package BEM++ [1].

The simulation of acoustic scattering with the combined field integral equation (CFIE) for the exterior Helmholtz equation becomes increasingly expensive for large wave numbers. To improve the efficiency of the iterative linear solver for high frequency scattering, the Laplace-Beltrami preconditioner will be used to reduce the condition number of the CFIE. This operator preconditioner is based on On-Surface Radiation Condition (OSRC) techniques and approximates the Neumann-to-Dirichlet map in the high-frequency range [2].

The Laplace-Beltrami preconditioner is a local operator and therefore results in a sparse system of linear equations that is efficient to solve with a direct method. Computational experiments show that the number of iterations to solve the preconditioned CFIE hardly grows for increasing wave number. The application of the Laplace-Beltrami preconditioner to the simulation of acoustic scattering on a rib cage confirms the feasibility for geometries of industrial interest.

### References

- [1] W. Śmigaj, S. Arridge, T. Betcke, J. Phillips, and M. Schweiger. “Solving Boundary Integral Problems with BEM++”, to appear in *ACM Transactions on Mathematical Software*, 2014.
- [2] M. Darbas, E. Darrigrand, and Y. Lafranche. “Combining analytic preconditioner and Fast Multipole Method for the 3-D Helmholtz equation”, *Journal of Computational Physics*, vol. 236, pp. 289–316, 2013.

## Shape optimization based on BEM and subdivision surfaces

Jan Zapletal, Michal Merta

IT4Innovations, VŠB-TU Ostrava, Czech Republic

The presented talk is concerned with numerical solution of shape optimization problems with constraints given by an elliptic partial differential equation. Our approach is based on the first-optimize-then-discretize approach, which results in the Hadamard-Zolésio form of the shape derivative given by a surface integral. This makes the boundary element method an efficient tool both for the solution of state and adjoint problems and the evaluation of the shape gradient.

To describe shape perturbations we use subdivision surfaces known, e.g., from computer graphics. While a fine-enough mesh is necessary for the boundary element analysis, the shape optimization is performed on a lower-resolution mesh representing the same limit surface. When an optimum is found on the current resolution, the control mesh is refined to describe finer details of the optimal surface.

To validate the method we present numerical experiments inspired by the Bernoulli free surface problem.

## Participants

1. Dominic Amann  
Institut für Numerische Mathematik, TU Graz, Steyrergasse 30, 8010 Graz  
`dominic.amann@student.tugraz.at`
2. Matthieu Aussal  
CMAP, École Polytechnique, Route de Saclay, 91128 Palaiseau CEDEX France  
`Matthieu.Aussal@gmail.com`
3. Dr. Timo Betcke  
Department of Mathematics, University College London,  
Gower Street, London WC1E 6BT, UK  
`t.betcke@ucl.ac.uk`
4. Monica Bugeanu  
Mathematisches Institut, Universität Basel,  
Rheinsprung 21, 4051 Basel, Switzerland  
`monica.bugeanu@unibas.ch`
5. Jürgen Dölz  
Mathematisches Institut, Universität Basel,  
Rheinsprung 21, 4051 Basel, Switzerland  
`juergen.doelz@unibas.ch`
6. Dipl.-Ing. Thomas Führer  
Institut für Analysis und Wissenschaftliches Rechnen, TU Wien,  
Wiedner Hauptstrasse 8–10, 1040 Wien, Austria  
`thomas.fuehrer@tuwien.ac.at`
7. Gregor Gantner  
Institut für Analysis und Wissenschaftliches Rechnen, TU Wien,  
Wiedner Hauptstrasse 8–10, 1040 Wien, Austria  
`e0826963@student.tuwien.ac.at`
8. Prof. Dr. Helmut Harbrecht  
Mathematisches Institut, Universität Basel,  
Rheinsprung 21, 4051 Basel, Switzerland  
`helmut.harbrecht@unibas.ch`
9. Prof. Dr. Stefan Kurz  
Department of Electronics, Electromagnetics,  
Tampere University of Technology, 33101 Tampere, Finland  
`stefan.kurz@tut.fi`
10. Dr. Dalibor Lukas  
Department of Applied Mathematics, VSB TU Ostrava,  
Trida 17, listopadu 15, 70833 Ostrava–Poruba, Czech Republic  
`dalibor.lukas@vsb.cz`

11. Lukas Maly  
Department of Applied Mathematics, VSB TU Ostrava,  
Trida 17, listopadu 15, 70833 Ostrava–Poruba, Czech Republic  
`lukas.maly@vsb.cz`
12. Dr. Günther Of  
Institut für Numerische Mathematik, TU Graz,  
Steyrergasse 30, 8010 Graz, Austria  
`of@tugraz.at`
13. Dr. Nicolas Salles  
Department of Mathematics, University College London,  
Gower Street, London WC1E 6BT, UK  
`n.salles@ucl.ac.uk`
14. Prof. Dr.–Ing. Martin Schanz  
Institut für Baumechanik, TU Graz,  
Technikerstrasse 4, 8010 Graz, Austria  
`m.schanz@tugraz.at`
15. Prof. Dr. Olaf Steinbach  
Institut für Numerische Mathematik, TU Graz,  
Steyrergasse 30, 8010 Graz, Austria  
`o.steinbach@tugraz.at`
16. Dr. Gerhard Unger  
Institut für Numerische Mathematik, TU Graz,  
Steyrergasse 30, 8010 Graz, Austria  
`gerhard.unger@tugraz.at`
17. Carolina A. Urzúa Torres  
Seminar for Applied Mathematics, ETH Zürich,  
Raemistrasse 101, 8092 Zürich, Switzerland  
`carolina.urzua@sam.math.ethz.ch`
18. Manuela Utzinger, M. Sc.  
Mathematisches Institut, Universität Basel,  
Rheinsprung 21, 4051 Basel, Switzerland  
`manuela.utzinger@unibas.ch`
19. Prof. Dr.–Ing. Dr. h.c. Wolfgang L. Wendland  
Institut für Angewandte Analysis und Numerische Simulation,  
Universität Stuttgart, Pfaffenwaldring 57, 70569 Stuttgart, Germany  
`wolfgang.wendland@mathematik.uni-stuttgart.de`
20. Dr.ir. Elwin van 't Wout  
Centre for Medical Image Computing, University College London  
`e.wout@ucl.ac.uk`

21. Jan Zapletal, M. Sc.  
IT4Innovations, VŠB-TU Ostrava, 17. listopadu 15/2172, 708 33,  
Czech Republic  
[jan.zapletal@vsb.cz](mailto:jan.zapletal@vsb.cz)

## **Erschienenene Preprints ab Nummer 2014/1**

- 2014/1 K. Bandara, F. Cirak, G. Of, O. Steinbach, J. Zapletal: Boundary element based multiresolution shape optimisation in electrostatics.
- 2014/2 T. X. Phan, O. Steinbach: Boundary integral equations for optimal control problems with partial Dirichlet control.
- 2014/3 M. Neumüller, O. Steinbach: An energy space finite element approach for distributed control problems.
- 2014/4 L. John, O. Steinbach: Schur complement preconditioners for boundary control problems.
- 2014/5 O. Steinbach: Partielle Differentialgleichungen und Numerik.
- 2014/6 T. Apel, O. Steinbach, M. Winkler: Error estimates for Neumann boundary control problems with energy regularization.
- 2014/7 G. Haase, G. Plank, O. Steinbach (eds.): Modelling and Simulation in Biomechanics. Book of Abstracts.